# Calculation of the difference between molar heat CAPACITY OF LIQUID AND IDEAL GAS FROM THE TEMPERATURE dependence of heat of vaporization* 

Vladimír Majer, Václav Svoboda and Jiří Pick<br>Department of Physical Chemistry,<br>Prague Institute of Chemical Technology, 16628 Prague 6

Received April I7h, 1978

A method was developed for calculating the difference $\Delta c_{P}$ between molar heat capacity of liquid $c_{\mathrm{P}}^{1}$ and of ideal gas $c_{\mathrm{P}}^{80}$ from the temperature dependence of heat of vaporization. By an a priori analysis the maximum error of the calculation procedure was determined. The exploitation of the method was demonstrated on a group of 20 saturated hydrocarbons. Besides these $\Delta c_{\mathbf{P}}$ values, the data on $c_{\mathrm{P}}^{1}$ and $c_{\mathrm{P}}^{\mathrm{go}}$ were calculated in the regions where no experimental data are available, by combining $\Delta c_{\mathrm{P}}$ with the experimental values of molar heat capacities.

The difference between the molar heat capacity of liquid $c_{\mathrm{P}}^{1}$ and the molar heat capacity of ideal gas $c_{\mathrm{P}}^{\mathrm{go}}$ is a thermodynamic quantity (denoted henceforth as $\Delta c_{\mathrm{P}}$ ) important for the thermodynamic description of vapour-liquid phase equilibrium. This quantity is useful when calculating the enthalpy balances of some engineering processes, it can be used further for mutual conversions between the molar heat capacity of liquid and that of ideal gas. The quantity $\Delta c_{p}$ has a close relation to the temperature derivative of heat of vaporization. In chemical-engineering relations for estimating $c_{\mathrm{P}}^{1}$ on the basis of the knowledge of $c_{\mathrm{P}}^{\mathrm{go}}$, however, the value $\Delta c_{\mathrm{P}}$ is usually calculated from the second-order derivative of saturated vapour pressures with respect to temperature ${ }^{1}$. Such a procedure is numerically badly stable and the calculation is usually subject to a considerable error. The calculation of $\Delta c_{\mathrm{p}}$ directly by using the temperature dependence of heat of vaporization, however, has not been applied yet above all for considerable lack of accurate experimental data on heat of vaporization which would enable to determine the derivative of heat of vaporization with respect to temperature with sufficient accuracy. In our laboratory we have been dealing for several years with the accurate measurements of heats of vaporization in their dependence on temperature. Therefore we decided to develop a method allowing to exploit these data for the determination of $\Delta c_{\mathrm{p}}$. The aim of this paper is to test the chosen method, to judge its accuracy, reliability and to delimit the region in which its reasonable application is possible. The calculations of $\Delta c_{\mathrm{P}}$ were demonstrated on a group of saturated hydrocarbons ( 16 aliphatic and 4 cyclic) $\mathrm{C} 5-\mathrm{C} 8$.

[^0]Hydrocarbons are very suitable for the first test of the method proposed because accurate data on heat of vaporization are available for them, it is possible to express comparatively easily the $\mathrm{P}-\mathrm{V}-\mathrm{T}$ behaviour of these substances and for some of them also experimental values $c_{\mathrm{P}}^{\mathrm{go}}$ and $c_{\mathrm{P}}^{1}$ may be found in the literature which can be employed for the comparison of $\Delta c_{\mathrm{P}}$ calculated from heats of vaporization with the values determined from experimental molar heat capacities.

## THEORETICAL

The change of heat of vaporization with temperature along the line of saturation (pressure and temperature are bound by the Clapeyron equation and designated by subscript $\sigma$ ) can be expressed by the following way

$$
\begin{gather*}
\left(\partial \Delta H_{\mathrm{V}} / \partial T\right)_{\sigma}=\left(\partial H^{\mathrm{g}} / \partial T\right)_{\mathrm{P}}+\left(\partial H^{\mathrm{g}} / \partial P\right)_{\mathrm{T}}(\partial P / \partial T)_{\sigma}+ \\
-\left(\partial H^{1} / \partial T\right)_{\mathrm{P}}-\left(\partial H^{1} / \partial P\right)_{\mathrm{T}}(\partial P / \partial T)_{\sigma} \tag{I}
\end{gather*}
$$

and by rearranging we obtain the relation

$$
\begin{align*}
\left(\partial \Delta H_{\mathrm{v}} / \partial T\right)_{\sigma} & =c_{\mathrm{P}}^{\mathrm{g}}-c_{\mathrm{P}}^{1}+\Delta H_{\mathrm{v}} / T\left[1-T\left(\left(\partial V^{\mathrm{g}} / \partial T\right)_{\mathrm{P}}+\right.\right. \\
& \left.\left.-\left(\partial V^{1} / \partial T\right)_{\mathrm{P}}\right) /\left(V^{\mathrm{g}}-V^{1}\right)\right] . \tag{2}
\end{align*}
$$

Considering that it holds

$$
\begin{equation*}
c_{\mathrm{P}}^{\mathrm{g}}-c_{\mathrm{P}}^{\mathrm{go}}=-T \int_{0}^{\mathrm{P}}\left(\partial^{2} V^{\mathrm{g}} / \partial T^{2}\right)_{\mathrm{P}} \mathrm{~d} P, \tag{3}
\end{equation*}
$$

it is possible by combining Eqs (2) and (3) to attain the expression giving the difference of molar heat capacity of liquid and ideal gas in the form

$$
\begin{gather*}
c_{\mathrm{P}}^{1}-c_{\mathrm{P}}^{\mathrm{go}}=-\left(\partial \Delta H_{\mathrm{v}} / \partial T\right)_{\mathrm{F}}+\Delta H_{\mathrm{v}} / T\left(1-T\left(\left(\partial V^{\mathrm{g}} / \partial T\right)_{\mathrm{P}}+\right.\right. \\
\left.\left.-\left(\partial V^{1} / \partial T\right)_{\mathrm{P}}\right) /\left(V^{\mathrm{g}}-V^{1}\right)\right)-T \int_{0}^{\mathrm{P}}\left(\partial^{2} V^{\mathrm{g}} / \partial T^{2}\right)_{\mathrm{P}} \mathrm{~d} P \tag{4}
\end{gather*}
$$

The accuracy of the first member on the right-hand side of Eq. (4) usually above all conditions the success of calculation and for simplicity it will be denoted further as $\mathrm{D} H_{\mathrm{v}}$. The values of next two terms increase with increasing non-ideality of the vapour phase and in further text they will be denoted as correction terms $D_{1}$ and $D_{2}$. Then holds

$$
\begin{equation*}
\Delta c_{\mathrm{P}}=-\mathrm{D} H_{\mathrm{v}}+D_{1}+D_{2} \tag{5}
\end{equation*}
$$

To express the first member $\mathrm{D} H_{\mathrm{v}}$ the data on temperature dependence of heat of vaporization were used which were published in the foregoing part of our series ${ }^{2}$. The given data set was obtained on the basis of critical analysis of literature values and of the results obtained recently in our laboratory. The data were selected which were considered to be the most accurate. In some cases the data of several authors were combined to attain wider temperature range and to diminish the probability of occurrence of systematic errors. The data were correlated by the Thiesen relation

$$
\begin{equation*}
\Delta H_{\mathrm{v}}=K\left(1-T_{\mathrm{r}}\right)^{\alpha} . \tag{6}
\end{equation*}
$$

In Table I, the values of constants of the Thiesen correlation relation $K(\mathrm{~kJ} / \mathrm{mol})$ and $\alpha$ are given for the substances investigated together with the temperature ranges within which they hold. We assume that it is possible to determine heat of vaporization with an accuracy of $0 \cdot 2 \%$ in terms of the given constants in the respective temperature ranges.

It is evident from Eq. (4) that for determining the correction terms $D_{1}$ and $D_{2}$ it is necessary to estimate as well the $\mathrm{P}-\mathrm{V}-\mathrm{T}$ behaviour of the liquid and above all of the vapour phase. Considering that temperatures within the range of 0 to $100^{\circ} \mathrm{C}$ and pressures altogether lower than 150 kPa are concerned in this work, the virial expansion truncated after the second virial coefficient was used to express the $\mathrm{P}-\mathrm{V}-\mathrm{T}$ behaviour of the vapour phase. Attention was paid to the choice of suitable relation for the second virial coefficient which would make it possible to express with sufficient accuracy above all the first- and second-order derivative of volume with respect to temperature. The fact that the results can be influenced to a considerable extent by the use of virial expansion explicit in pressure or volume has been discussed before ${ }^{3}$. It was found by an analysis carried out by us that in the given case it is most advantageous to make use of the pressure-explicit form of virial equation where the value of second virial coefficient is determined according to Pitzer and Curl ${ }^{4}$. This estimation relation is especially advantageous for our case because when evaluating constants of this equation, experimental data on pressure dependence of $c_{\mathrm{P}}^{8}$ of some hydrocarbons had been used, too.
To express molar volume of the liquid phase the Rackett equation ${ }^{5}$ was used

$$
\begin{gather*}
V^{1}=\left(R T_{\mathrm{c}} / P_{\mathrm{c}}\right) z_{\mathrm{c}}^{\left[1+\left(1-T_{\mathrm{r}}\right)^{0.28571]}\right.}  \tag{7}\\
\left(\partial V^{1} / \partial T\right)_{\mathrm{p}}=-0.28571 V^{1} \ln \left(V^{1}\right)\left(1-T_{\mathrm{r}}\right)^{0.28571} /\left(T_{\mathrm{c}}-T\right) . \tag{8}
\end{gather*}
$$

The terms in Eq. (5) can be then expressed as follows:

$$
\begin{equation*}
\mathrm{D} H_{\mathrm{v}}=-\alpha \Delta H_{\mathrm{v}} /\left(T_{\mathrm{c}}-T\right), \tag{9}
\end{equation*}
$$

TABLE I
Constants of Correlation Relations $\Delta H_{\mathrm{v}}=K\left(1-T_{\mathrm{r}}\right)^{\boldsymbol{a}}$ and $\Delta c_{\mathrm{P}}=K_{0}+K_{1} T+K_{2} T^{2}+K_{3} T^{3}$

| Substance | K | $\alpha$ | $K_{0}$ | $K_{1} \cdot 10^{3}$ | $K_{2} \cdot 10^{6}$ | $K_{3} \cdot 10^{9}$ | Temperature range, ${ }^{\circ} \mathrm{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pentane | 38.58 | 0.375 | -191.371 | 2394.46 | -8106.82 | $9346 \cdot 67$ | 25-80 |
| 2-Methylbutane | $36 \cdot 36$ | 0.365 | -161.151 | 2118.123 | -7372.67 | 8738.77 | 6-28 |
| Hexane | 43.97 | 0.375 | -131.434 | 1671.70 | -5 214.58 | 5594.54 | 25-80 |
| 2-Methylpentane | 42.04 | 0.373 | -138.278 | $1765 \cdot 63$ | -5 648.46 | $6197 \cdot 56$ | 25-60 |
| 3-Methylpentane | 42.03 | 0.367 | -140.176 | $1754 \cdot 19$ | - 5555.27 | $6025 \cdot 57$ | 25-80 |
| 2,2-Dimethylbutane | 39.07 | 0.366 | -127.048 | 1673.65 | - 5511.39 | $6207 \cdot 37$ | 23-50 |
| 2,3-Dimethylbutane | 39.85 | 0.346 | -117.242 | 1514.28 | -4838.74 | 5288.75 | 23-60 |
| Heptane | $50 \cdot 11$ | 0.393 | - 70.6846 | 1049.27 | -2983.95 | $3008 \cdot 83$ | 25-90 |
| 2-Methylhexane | 48.42 | 0.398 | - 76.5763 | 1127.09 | -3 298.10 | $3403 \cdot 13$ | 25-80 |
| 3-Methylhexane | 47.99 | 0.386 | - 66.5903 | 1004.76 | -2887.71 | 2931.31 | 25-80 |
| 2,3-Dimethylpentane | $46 \cdot 28$ | $0 \cdot 372$ | - 64.9402 | 969.247 | -2 $805 \cdot 15$ | 2856.78 | 25-80 |
| 2,2,3-Trimethylbutane | 43.72 | 0.377 | - 95.6909 | 1263.72 | -3795.12 | 3938.88 | 40-80 |
| Octane | 56.24 | 0.411 | - 5.8167 | 436.766 | - 953.328 | 822.620 | 25-80 |
| 2-Methylheptane | 54.30 | 0.413 | - 23.9006 | 613.649 | -1 536.91 | 1447.49 | 25-80 |
| 4-Methylheptane | 54.29 | 0.414 | - 23.1073 | 605.683 | -1513.49 | 1421.24 | 25-80 |
| 2,2,4-Trimethylpentane | 47.33 | 0.375 | - 67.3557 | 984.072 | $-2817 \cdot 22$ | 2836.97 | 25-80 |
| Cyclopentane | 39.21 | 0.364 | - $82 \cdot 1108$ | 1163.08 | -3685.78 | 4016.51 | 25-50 |
| Methylcyclopentane | $43 \cdot 12$ | 0.378 | - 72.5517 | $1050 \cdot 00$ | -3157.52 | 3296.64 | 25-72 |
| Cyclohexane | $44 \cdot 10$ | 0.383 | - 60.4179 | 901.149 | -2622.59 | 2657.74 | 25-80 |
| Methylcyclohexane | 46.90 | 0.384 | - 30.2960 | 606.497 | -1626.04 | 1560.90 | 25-80 |

[^1]\[

$$
\begin{equation*}
D_{1}=\Delta H_{v} / T\left\{1-T\left[\boldsymbol{R} / P+\mathrm{d} B / \mathrm{d} T-\left(\partial V^{1} / \partial T\right)_{\mathrm{P}}\right] /\left(\boldsymbol{R} T / P+B-V^{1}\right)\right\}, \tag{10}
\end{equation*}
$$

\]

$$
\begin{equation*}
D_{2}=-T P\left(\mathrm{~d}^{2} B / \mathrm{d} T^{2}\right) . \tag{11}
\end{equation*}
$$

Possibilities of the method proposed were first justified on the basis of an a priori estimate of possible error in calculated values of $\Delta c_{\mathrm{p}}$. For such an estimation it is necessary to know at least approximately the magnitude and error of the three members occurring on the right-hand side of Eq. (5). The terms $\mathrm{D} H_{\mathrm{v}}, D_{1}$ and $D_{2}$ and the final values of $\Delta c_{\mathrm{P}}$ for normal hydrocarbons in their dependence on temperature are given in Table II for illustration. It clearly follows from the table that the importance of estimated terms $D_{1}$ and $D_{2}$ increases with rising temperature so increasing also the inaccuracy in $\Delta c_{\mathrm{p}}$. Heats of vaporization are known for most substances in the range not exceeding very much the temperature of normal boiling

Table II
Members of Eq. (5) in Dependence on Temperature for Normal Hydrocarbons ( $\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$ )

| Temperature ${ }^{\circ} \mathrm{C}$ | $\mathrm{D} H_{\mathrm{v}}$ | $D_{1}$ | $D_{2}$ | $c_{\mathrm{P}}^{1}-c_{\mathrm{P}}^{80}$ |
| :---: | :---: | :---: | :---: | :---: |
| Pentane |  |  |  |  |
| 10 | $-54.9$ | $-8.5$ | $2 \cdot 4$ | 48.8 |
| 40 | $-61 \cdot 2$ | -14.9 | $4 \cdot 1$ | $50 \cdot 5$ |
| 70 | -70.0 | $-22.9$ | $6 \cdot 4$ | $53 \cdot 5$ |
| Hexane |  |  |  |  |
| 10 | $-54.1$ | $-4.7$ | $1 \cdot 4$ | $50 \cdot 8$ |
| 40 | -59.2 | - 9.3 | $2 \cdot 6$ | $52 \cdot 5$ |
| 70 | -65.8 | -15.9 | $4 \cdot 3$ | $54 \cdot 2$ |
| Heplane |  |  |  |  |
| 10 | $-57.2$ | $-2.5$ | 0.7 | 55.5 |
| 40 | -61.7 | $-5.6$ | $1 \cdot 6$ | 57.7 |
| 70 | $-67.2$ | $-10.6$ | $2 \cdot 9$ | 59.6 |
| Octane |  |  |  |  |
| 10 | -61.0 | $-1.2$ | $0 \cdot 4$ | $60 \cdot 1$ |
| 40 | -65.1 | -3.3 | 0.9 | $62 \cdot 7$ |
| 70 | $-70 \cdot 1$ | --6.9 | 1.9 | 65.0 |

point. To estimate the maximum error it is therefore possible to start from the magnitude of values of input properties in the vicinity of normal boiling point. For the maximum error of $\Delta c_{\mathrm{P}}$ then holds

$$
\begin{equation*}
\delta \Delta c_{\mathrm{P}}=\delta \mathrm{D} H_{\mathrm{v}}+\delta D_{1}+\delta D_{2} . \tag{12}
\end{equation*}
$$

The error in $\Delta H_{v}$ was estimated at $0 \cdot 2 \%$ and therefore we can assume that the relative error $\delta_{\mathrm{r}} \mathrm{D} H_{\mathrm{v}}$ in the derivative of heat of vaporization will be about $0.5 \%$; for an average value $\mathrm{D} H_{\mathrm{v}}=66 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ the absolute error will be then about $\delta \mathrm{D} H_{\mathrm{v}}=0.33$ $\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$. When estimating the error of the member $D_{1}$ we can consider as typical the following values of input properties (in parentheses the estimated inaccuracy in per cent is always given): $B=-1300 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}(10 \%), \mathrm{d} B / \mathrm{d} T=10 \mathrm{~cm}^{3}$. $. \mathrm{mol}^{-1} \mathrm{~K}^{-1}(15-20 \%), V^{1}=150 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}(3 \%),\left(\delta V^{1} / \partial T\right)_{\mathrm{P}}=0.2 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. $\mathrm{K}^{-1}(6 \%), T=340 \mathrm{~K}$. Under these circumstances the relative error $\delta_{\mathrm{r}} D_{1}$ is then about $14 \%$ and for an average value of $D_{1}=16 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ the upper limit of error is $\delta D_{1}=2.2 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$. By comparing the values of the member $D_{2}$ calculated according to Eq. (1I) with the experimental data on $c_{\mathrm{P}}^{8}-c_{\mathrm{P}}^{80}$ given by Waddington and coworkers for some of substances investigated it followed that the error $\delta_{\mathrm{r}} D_{2}$ did not exceed $20 \%$; for a typical value of $D_{2}$ in the vicinity of the temperature of normal boiling point equal to $4 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ it is to be expected that $\delta D_{2}=0.8$ $\mathrm{J}_{\mathrm{mol}}{ }^{-1} \mathrm{~K}^{-1}$.

By adding the individual absolute errors of members of Eq. (12) we get $\delta \Delta c_{\mathrm{P}}=3.3$ $\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$. Assuming that $\Delta c_{\mathrm{P}}$ is on the average $54 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ it is then an error approximately $6 \%$. In this connection it is necessary to emphasize that the error determined by this a priori analysis is the upper limit of the error which may occur just under the assumption that all inaccuracies of input quantities will sum up in one direction. With regard to a considerable number of input data it is, however, very little statistically probable. In reality practically always a compensation of some inaccuracies occurs and the results are generally subject to a lower error. The error also decreases substantially with decreasing temperature owing to the decreasing significance of the terms $D_{1}$ and $D_{2}$. In the region about the pressure of saturated vapour equal to 50 kPa , the maximum limit of the error determined by the abovementioned way is already $\delta \Delta c_{\mathrm{P}}=1.9 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}, \delta_{\mathrm{r}} \Delta c_{\mathrm{P}}=3.5 \%$. When the value of $\Delta c_{\mathrm{P}}$ is employed for calculating $c_{\mathrm{P}}^{\mathrm{g}}\left(c_{\mathrm{P}}^{1}\right)$ on the basis of knowledge of experimental values $c_{\mathrm{P}}^{1}\left(c_{\mathrm{p}}^{\mathrm{g}}\right)$ the inaccuracy in the value $\Delta c_{\mathrm{p}}$ can cause a maximum error in $c_{\mathrm{P}}^{\mathrm{go}}\left(c_{\mathrm{P}}^{1}\right) 2 \%(1 \cdot 5 \%)$. We assume that for temperatures about normal boiling point the values $c_{\mathrm{P}}^{\mathrm{go}}=160 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ and $c_{\mathrm{P}}^{1}=210 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ are typical of the set of substances investigated.

## RESULTS

The results of calculating the difference between molar heat capacity of liquid and ideal gas $\Delta c_{\mathrm{P}}$ are summarized in Table I in the form of constants of the correlation polynomial $\Delta c_{\mathrm{P}}=K_{0}+K_{1} T+K_{2} T^{2}+K_{3} T^{3}\left(\mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right)$. The values $\Delta c_{\mathrm{P}}$ calculated from the temperature dependence of heat of vaporization are compared in Table III with the values determined from the experimental molar heat capacities $c_{\mathrm{P}}^{1}$ and $c_{\mathrm{P}}^{\mathrm{go}}$. The comparison was carried out for those substances for which a temperature range exists where the heats of vaporization and experimental values of $c_{\mathrm{P}}^{1}$ and $c_{\mathrm{P}}^{\mathrm{go}}$ are known simultaneously or their slight extrapolation is sufficient. In the second and third column, the absolute average deviations $\delta \Delta c_{\mathrm{p}}$ and the relative average deviations $\delta_{\mathrm{r}} \Delta c_{\mathrm{P}}$ of calculated values of $\Delta c_{\mathrm{P}}$ from experimental ones are given together with the temperature ranges where the comparison was carried out.

By combining the values $\Delta c_{\mathrm{P}}$ determined from the temperature dependence of heat of vaporization with the experimental values of $c_{\mathrm{P}}^{80}$ and $c_{\mathrm{P}}^{1}$ and on using the relations $c_{\mathrm{P}}^{1}=c_{\mathrm{P}, \mathrm{Exp}}^{\mathrm{go}}+\Delta c_{\mathrm{P}}$ and $c_{\mathrm{P}}^{\mathrm{go}}=c_{\mathrm{P}, \mathrm{Exp}}^{1}-\Delta c_{\mathrm{P}}$, the data on $c_{\mathrm{P}}^{1}$ and $c_{\mathrm{P}}^{\mathrm{go}}$ were obtained which reach to the temperature regions where no experimental data are known. The results are summarized in Table IV for all the set of substances investigated in the form of constants of the correlation polynomial $c_{\mathrm{P}}=K_{0}^{\prime}+K_{1}^{\prime} T+K_{2}^{\prime} T^{2}$. If the values of constants of the expansion for $c_{\mathrm{P}}^{1}$ are not given for some substances it means that no sufficiently accurate values of $c_{\mathrm{P}}^{\mathrm{go}}$ were found in the literature allowing the con-

## Table III

Deviations of Values $\Delta c_{P}$ Calculated from Temperature Dependence of Heat of Vaporization from Values Determined from Experimental Data on $c_{\mathrm{P}}^{1}$ and $c_{\mathrm{P}}^{\mathrm{go}}$

| Substance | $\bar{\delta} \Delta c_{\mathbf{P}}$ <br> $\mathbf{J} \mathrm{mol}^{-1} \mathbf{K}^{-1}$ | $\bar{\delta}_{\mathbf{r}} \Delta c_{\mathbf{P}}$ <br> $\%$ | Temp. range of <br> comparison, ${ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :---: | :---: |
|  | $0 \cdot 5$ | $0 \cdot 9$ | $5-25$ |
| Pentane | $1 \cdot 0$ | $2 \cdot 6$ | $30-40$ |
| 2-Methylbutane | $0 \cdot 5$ | $0 \cdot 9$ | $40-80$ |
| Hexane | $0 \cdot 7$ | $1 \cdot 3$ | $35-45$ |
| 2-Methylpentane | $0 \cdot 2$ | $0 \cdot 4$ | $40-50$ |
| 3-Methylpentane | $1 \cdot 5$ | $3 \cdot 2$ | $40-50$ |
| 2,2-Dimethylbutane | $3 \cdot 3$ | $6 \cdot 7$ | $35-55$ |
| 2,3-Dimethylbutane | $2 \cdot 8$ | $4 \cdot 8$ | $70-100$ |
| Heptane | $1 \cdot 1$ | $2 \cdot 3$ | $40-60$ |
| 2,2,3-Trimethylbutane | $0 \cdot 9$ | $2 \cdot 1$ | $35-45$ |
| Cyclopentane | $0 \cdot 2$ | $0 \cdot 5$ | $40-50$ |
| Methylcyclopentane | $1 \cdot 3$ | $2 \cdot 8$ | $85-95$ |
| Cyclohexane |  |  |  |

Table IV
Constants of Correlation Polynomial for Calculated Values of $c_{P}^{1}$ a $c_{P}^{\mathrm{go}}\left(\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}\right)$

| Substance | Value | $K_{0}^{\prime}$ |  | $K_{1}^{\prime} \cdot 10^{3}$ | $K_{2}^{\prime} \cdot 10^{6}$ | Temp range, ${ }^{\circ} \mathrm{C}$ | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pentane | $c_{\text {P }}^{1}$ | 47.3947 |  | 408.571 |  | 25-55 | 6 |
|  | ${ }^{\text {c }}{ }^{80}$ | 162.276 | - | $646 \cdot 132$ | 1688.35 | 5-55 | 7 |
| 2-Methylbutane | $c_{\text {p }}$ | 43.0877 |  | 410 |  | 30-40 | 8 |
|  | $c^{\mathrm{po}}$ | 35.636 |  | 276.935 |  | -5-40 | 9 |
| Hexane | $c_{\text {P }}$ | 58.6759 |  | 453.219 |  | 40-90 | 10 |
|  | $c_{\mathrm{P}}^{\mathrm{go}}$ | 139.189 | - | 281.748 | 1000 | $5-85$ | 7 |
| 2-Methylpentane | $c_{P}^{1}$ | 55.1935 |  | 462.667 |  | 35-75 | 11 |
|  | $c_{\text {P }}{ }^{\text {¢ }}$ | 45.5708 |  | 328.333 |  | 10-45 | 12 |
| 3-Methylpentane | $c^{1}$ | 51.04 |  | 462.969 |  | $40-85$ | 11 |
|  | $c_{\text {P }}^{80}$ | $45 \cdot 1912$ |  | $325 \cdot 413$ |  | $5-50$ | 12 |
| 2,2-Dimethylbutane | $c_{\text {P }}^{1}$ | 44.2829 |  | 480.001 |  | 40-60 | 10 |
|  | $c_{P}^{\mathrm{go}}$ | - 29.8659 |  | 846.9 | - 904.748 | $10-50$ | 12 |
| 2,3-Dimethylbutane | $c_{p}^{1}$ | 44.4538 |  | 467.857 |  | $40-70$ | 11 |
|  | $c_{P}^{p 0}$ | 94.5522 | - | 9.08899 | $591 \cdot 193$ | $10-55$ | 12 |
| Heptane | $c_{P}^{l}$ | 63.9054 |  | 526.787 |  | 65-100 | 13 |
|  | $c^{80}$ | 155.865 | - | 211.449 | 847.824 | 5-100 | 7 |
| 2-Methylhexane | $c_{\text {Po }}^{\text {go }}$ | 154.341 | - | 287.067 | 1099.63 | $5-45$ | 14 |
| 3-Methylhexane | $c_{\text {Po }}^{\text {go }}$ | 342.879 |  | 1639.63 | 3493.59 | 5-45 | 15 |
| 2,3-Dimethylpentane | $c_{\text {Po }}^{\text {go }}$ | 237.202 | - | 882.838 | 2166.63 | 5-40 | 15 |
| 2,2,3-Trimethylbutane | $c_{p}^{\text {! }}$ | 52.2595 |  | 535.667 |  | $40-80$ | 13 |
|  | $c_{\text {Po }}$ | 47.3591 |  | 395.667 |  | 25-65 | 14 |
| Octane | $c_{\text {Po }}^{\text {go }}$ | 183.487 | - | 217.566 | 812.725 | 5-100 | 7 |
| 2-Methylheptane | $c_{\text {Po }}^{\text {go }}$ | 82.9531 |  | 361.711 |  | $5-60$ | 16 |
| 4-Methylpentane | $c^{\text {goo }}$ | 113.586 |  | 99.0779 | 532.024 | 5-60 | 16 |
| 2,2,4-Trimethylpentane | $c_{\mathrm{P}}^{\mathrm{go}}$ | $-153.785$ |  | 1878.02 | -2 $451 \cdot 6$ | $5-60$ | 16 |
| Cyclopentane | $c_{p}^{1}$ | 6.08292 |  | 402.725 |  | 35-60 | 17 |
|  | $c_{\text {P }}{ }^{\text {go }}$ | - 0.462498 |  | $280 \cdot 133$ |  | 15-45 | 18 |
| Methylcyclopentane | $c_{\text {P }}^{1}$ | 21.7152 |  | 453.992 |  | 40-85 | 17 |
|  | $c_{p}^{\text {ko }}$ | 77.8392 | - | 90.8065 | 683-198 | $10-50$ | 18 |
| Cyclohexane | $c_{p}^{1}$ | 51.8587 |  | 364.881 |  | 80-100 | 19 |
|  | $c_{\text {P }}{ }^{\text {Po }}$ | 63.2925 | - | 10.8584 | 571.929 | 5-100 | 20-22 |
| Methylcyclohexane | $c_{\text {Po }}$ | 116.882 | - | 230.786 | $1005 \cdot 9$ | $5-55$ | 23 |

version mentioned. In other columns, the temperature ranges are given in which the constants hold and references from which the experimental values of $c_{\mathrm{P}, \mathrm{Exp}}^{\mathrm{go}}\left(c_{\mathrm{P}, \mathrm{ExP}_{\mathrm{P}}}^{1}\right)$ for calculation of $c_{\mathrm{P}}^{1}\left(c_{\mathrm{P}}^{80}\right)$ were taken over.

## DISCUSSION

When judging the applicability and accuracy of the method developed it is necessary to take into account the present state of our knowledge of experimental molar heat capacities of liquids and gases. The up-to-date adiabatic calorimetry is able to provide values of molar heat capacities of liquids within the range from very low temperatures up to a temperature $20-30^{\circ} \mathrm{C}$ below normal boiling point with an accuracy better than to $0.5 \%$, the best laboratories report even the error lower than $0.2 \%$. In the vicinity of the temperature of normal boiling point, however, the scattering of values given for the same substance by different authors is usually considerable (often $1-2 \%$ ). The experiments are commonly, in the region of higher saturated vapour pressures, subject to systematic errors usually due to evaporation effects. The values of molar heat capacities of ideal gas are most often determined by calculating from spectra; however, these data do not often correspond to the real values of $c_{\mathrm{P}}^{\mathrm{go}}$ because even for not too complicated molecules it is not possible to determine and resolve all fundamental vibrations and to establish the values of energy barriers which influence the value of gas molar heat capacity especially in the region of lower temperatures. The direct calorimetric determination of $c_{\mathrm{P}}^{80}$ by extrapolating molar heat capacities measured at several pressures to the value of zero pressure is experimentally rather troublesome. Some authors attain the accuracy of as much as $0.2 \%$ by elaborating this method; however, small number of systems in not too wide temperature ranges has been measured in this way for the present and generally the values of $c_{\mathrm{P}}^{\mathrm{go}}$ determined from spectral data are preferred. It follows unambiguously from the Touloukian and Makita critical compilation ${ }^{7}$, summarizing all the data on molar heat capacities of 55 industrially and theoretically important substances, that at high temperatures the agreement among the authors reporting $c_{\mathrm{P}}^{\mathrm{go}}$ of organic substances is usually good but at temperatures around normal boiling point the scattering is always $3-4 \%$ and with decreasing temperature it has yet increasing trend.

It follows from the above-mentioned facts that the values $\Delta c_{\mathrm{P}}$ determined from experimental values of molar heat capacities can be liable to a considerable uncertainty (several per cent) which can strongly exceed the sum of errors in molar heat capacity of liquid and gas given by authors. Under these conditions it is then possible to consider the values of $\Delta c_{\mathrm{P}}$ calculated from the temperature dependence of heat of vaporization, as very good. This confirms also the altogether satisfactory agreement of experimental and calculated values of $\Delta c_{p}$.

If the values $\Delta c_{\mathrm{p}}$ are calculated from beats of vaporization by the way indicated they can be easily used for conversions between molar heat capacity of ideal gas
and liquid. It enables an advantageous estimate in the regions where one of the quantities mentioned is experimentally accessible with difficulty while the second is known with sufficient accuracy. The concrete calculations and the presented survey of the contemporary knowledge of experimental $c_{\mathrm{p}}$ data indicate under which circumstances is advantageous to exploit such a type of conversions. The combination of $\Delta c_{\mathrm{P}}$ with an experimental value of $c_{\mathrm{P}}^{1}$ is suitable for estimating $c_{\mathrm{P}}^{\mathrm{go}}$ at temperatures far below the temperature of normal boiling point because the values of molar heat capacity of liquid are known here with sufficient accuracy, while it is not possible to obtain here reliable data on $c_{\mathrm{P}}^{\mathrm{go}}$. On the other hand the calculation of $c_{\mathrm{P}}^{1}$ on the basis of combination of $\Delta c_{\mathrm{P}}$ with experimental value of $c_{\mathrm{P}}^{\mathrm{go}}$ can be used at temperatures around normal boiling point where the determination of molar heat capacity of liquids is complicated and of little reliability.

## LIST OF SYMBOLS

| $B$ | second virial coefficient |
| :--- | :--- |
| $c_{\mathrm{P}}$ | molar heat capacity at constant pressure |
| $\Delta c_{\mathrm{P}}$ | difference between molar heat capacity of liquid and ideal gas |
| $D_{1}, D_{2}$ | corrrection terms defined by Eqs (10) and (1l) |
| $D H_{\mathrm{v}}$ | deivative of heat of vaporization with respect to temperature |
| $H$ | molar enthalpy |
| $\Delta H_{\mathrm{v}}$ | heat of vaporization |
| $K$ | adjustable constant of Thiesen relation |
| $K_{0}-K_{3}$ | adjustable constants of polynomial for expressing $\Delta c_{\mathrm{P}}$ |
| $K_{0}^{\prime}-K_{2}^{\prime}$ | adjustable constants of polynomial for expressing $c_{\mathrm{P}}$ |
| $P$ | pressure |
| $R$ | gas constant |
| $T$ | temperature (K) |
| $V$ | molar volume |
| $z$ | compressibility factor |
| $\alpha$ | adjustable constant of Thiesen relation |
| $\delta$ | absolute deviation |
| $\bar{\delta}$ | average absolute deviation |
| $\delta_{\mathrm{r}}$ | relative deviation |
| $\bar{\delta}_{\mathrm{r}}$ | average relative deviation |

## Indices

| c | critical property |
| :--- | :--- |
| g | vapour property |
| go | ideal-gas property |
| J | liquid property |
| r | reduced quantity |
| $\sigma$ | change along saturation line |

## REFERENCES

1. Reid R. C., Prausnitz J. M.; Sherwood T. K.: The Properries of Gases and Liquids, 3rd Edition. McGraw-Hill, New York 1977.
2. Majer V., Svoboda V., Hála S., Pick J.: This Journal, in press.
3. Majer V.: Thesis. Prague Institute of Chemical Technology, Prague 1973.
4. Pitzer K. S., Curl R. F.: J. Amer. Chem. Soc. 79, 2369 (1957).
5. Rackett H. G.: J. Chem. Eng. Data 15, 514 (1970).
6. Pitzer K. S.: J. Amer. Chem. Soc. 63, 2413 (1941).
7. Touloukian Y. S., Makita T.: Specific Heat, Nonmetallic Liquids and Gases. 1F1/Plenum, New York 1970.
8. Scott D. W., McCullough J. P., Williamson K. D., Waddington G.: J. Amer. Chem. Soc. 73, 1707 (1951).
9. Gurthie G. B., Huffmann H. M.: J. Amer. Chem. Soc. 65, 1139 (1943).
10. Waddington G., Douslin D. R.: J. Amer. Chem. Soc. 69, 2275 (1947).
11. Waddington G., Smith J. C., Scott D. W., Huffmann H. M.: J. Amer. Chem. Soc. 71, 3902 (1949).
12. Douslin D. R., Huffmann H. M.: J. Amer. Chem. Soc. 68, 1704 (1946).
13. Waddington G., Todd S. S., Huffmann H. M.: J. Amer. Chem. Soc. 69, 22 (1947).
14. Huffmann H. M., Gross M. E., Scott D. W., McCutlogh J. P.: J. Phys. Chem. 65, 495 (1961).
15. Huffmann H. N., Parks G. S., Thomas S. B.: J. Amer. Chem. Soc. 52, 3241 (1930).
16. Osborne N. S., Ginnings D. C.: J. Res. Nat. Bur. Stand., Sect. A 39, 453 (1947).
17. McCullogh J. P., Pennington R. F., Smith J. C., Hossenlopp I. A., Waddington G.: J. Amer. Chem. Soc. 81, 5880 (1959).
18. Douslin R. P., Huffmann H. M.: J. Amer. Chem. Soc. 68, 174 (1946).
19. Spitzer R., Pitzer K. S.: J. Amer. Chem. Soc. 68, 2537 (1946).
20. Moelwyn-Hughes E. A., Thorpe P. L.: Proc. Roy. Soc., Ser A 278, 578 (1963).
21. Klesper I.: Z. Phys. Chem. (Frankfurt am Main) 51, 1 (1966).
22. Wilhelm F., Zettler M., Sackmann H.: Ber. Bunsenges. Phys. Chem. 78, 795 (1974).
23. Holzhauer J. K., Ziegler W. T.: J. Phys. Chem. 79, 590 (1975).
[^2]
[^0]:    * Part XIII in the series Enthalpy Data of Liquids; Part XIII: This Journal 44, 637 (1979).

[^1]:    ${ }^{a}$ Values of constants are given for $\Delta H_{\mathrm{v}}$ in $\mathrm{kJ} \mathrm{mol}^{-1}$ and $\Delta c_{\mathrm{p}}$ in $\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$.

[^2]:    Translated by J. Linek.

